# Building Java Programs

read: 12.5

Recursive backtracking

### **Exhaustive Search**

- Iterate through all elements of a search space
- Useful to solve problems that require making decisions
  - Each decision leads to new choices
  - Insufficient information to make a thoughtful choice
- Depth first search: we go deep down one path rather than broad
- Natural to implement recursively: call stack keeps track of decision points in right order (opposite from visited)

### Exercise: Permutations

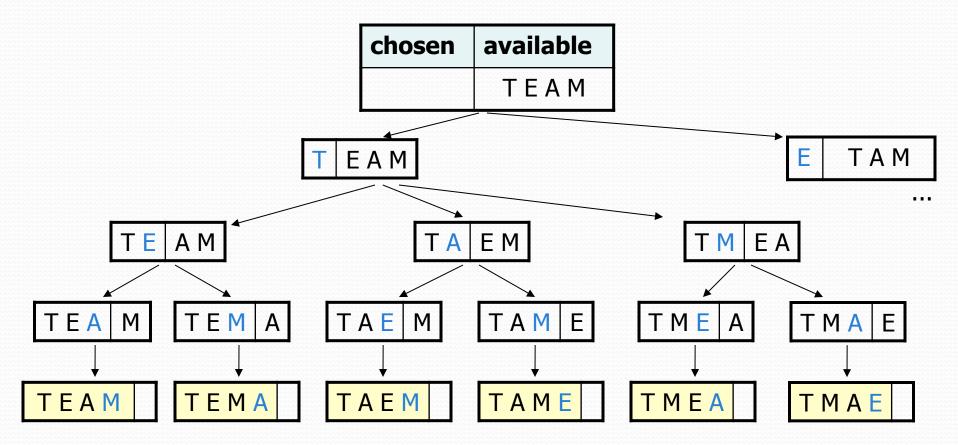
- Write a method permute that accepts a string as a parameter and outputs all possible rearrangements of the letters in that string. The arrangements may be output in any order.
  - Example: permute("TEAM") outputs the following sequence of lines:

TEAM	ATEM
TEMA	ATME
TAEM	AETM
TAME	AEMT
TMEA	AMTE
TMAE	AMET
ETAM	MTEA
ETMA	MTAE
EATM	META
EAMT	MEAT
EMTA	MATE
EMAT	MAET

## Examining the problem

- Each permutation is a set of choices or decisions:
  - Which character do I want to place first?
  - Which character do I want to place second?
  - . . .
  - solution space: set of all possible sets of decisions to explore

## Decision tree



## Exercise solution

```
// Outputs all permutations of the given string.
public static void permute(String s) {
    permute(s, "");
private static void permute(String s, String chosen) {
    if (s.length() == 0) {
        // base case: no choices left to be made
        System.out.println(chosen);
    } else {
        // recursive case: choose each possible next letter
        for (int i = 0; i < s.length(); i++) {
            char c = s.charAt(i);
            s = s.substring(0, i) + s.substring(i + 1);
            chosen += c;
            permute(s, chosen);
                                                 // explore
            s = s.substring(0, i) + c + s.substring(i);
            chosen = chosen.substring(0, chosen.length() - 1);
                                                 // un-choose
```

## Exercise solution 2

```
// Outputs all permutations of the given string.
public static void permute(String s) {
    permute(s, "");
private static void permute(String s, String chosen) {
    if (s.length() == 0) {
        // base case: no choices left to be made
        System.out.println(chosen);
    } else {
        // recursive case: choose each possible next letter
        for (int i = 0; i < s.length(); i++) {
            String ch = s.substring(i, i + 1); // choose
            String rest = s.substring(0, i) + // remove
                          s.substring(i + 1);
            permute(rest, chosen + ch);
                                               // explore
            // (don't need to "un-choose" because
            // we used temp variables)
```

## Backtracking

- Useful to solve problems that require making decisions
  - Each decision leads to new choices
  - Some (but not all!) sequence(s) of choices will be a solution
  - Insufficient information to make a thoughtful choice
- Systematically prune out infeasible solutions

## Backtracking strategies

- When solving a backtracking problem, ask these questions:
  - What are the "choices" in this problem?
    - What is the "base case"? (How do I know when I'm out of choices?)
  - How do I "make" a choice?
    - Do I need to create additional variables to remember my choices?
    - Do I need to modify the values of existing variables?
  - How do I explore the rest of the choices?
    - Do I need to remove the made choice from the list of choices?
  - Once I'm done exploring, what should I do?
  - How do I "un-make" a choice?

## Maze class

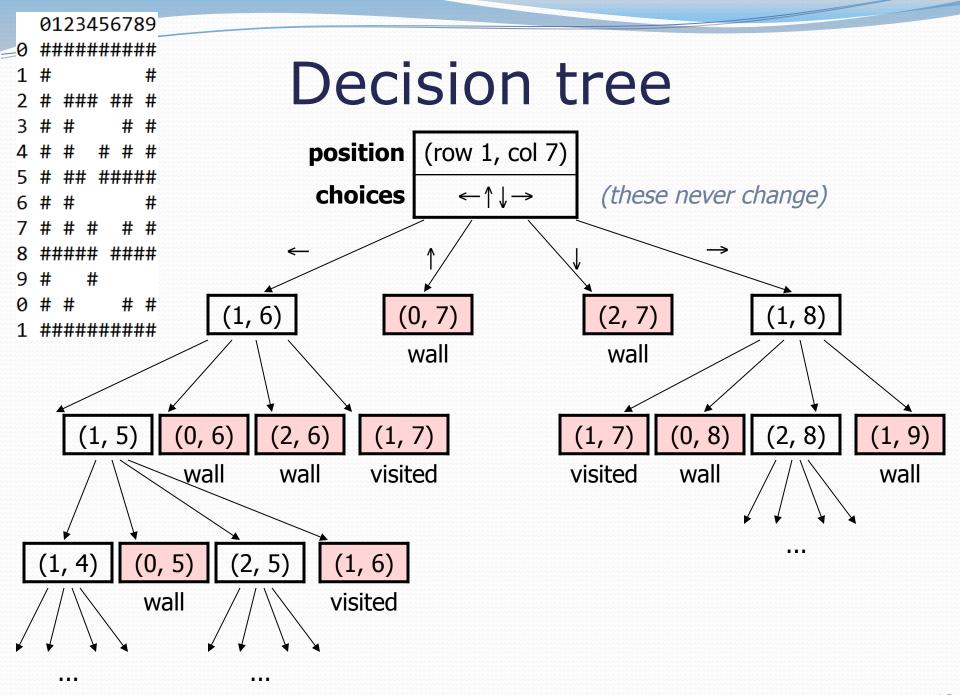


• Suppose we have a Maze class with these methods:

Method/Constructor	Description
public Maze(String text)	construct a given maze
<pre>public int getHeight(), getWidth()</pre>	get maze dimensions
<pre>public boolean isExplored(int r, int c) public void setExplored(int r, int c)</pre>	get/set whether you have visited a location
public void <b>isWall</b> (int r, int c)	whether given location is blocked by a wall
<pre>public void mark(int r, int c) public void isMarked(int r, int c)</pre>	whether given location is marked in a path
<pre>public String toString()</pre>	text display of maze

### Exercise: solve maze

- Write a method solveMaze that accepts a Maze and a starting row/column as parameters and tries to find a path out of the maze starting from that position.
  - If you find a solution:
    - Your code should stop exploring.
    - You should mark the path out of the maze on your way back out of the recursion, using backtracking.
  - (As you explore the maze, squares you set as 'explored' will be printed with a dot, and squares you 'mark' will display an X.)



## Recall: Backtracking

A general pseudo-code algorithm for backtracking problems:

#### Explore(choices):

- if there are no more choices to make: stop.
- else, for each available choice C:
  - Choose C.
  - Explore the remaining choices.
  - Un-choose C, if necessary. (backtrack!)

What are the choices in this problem?